

AD-A126 339

SOME NEW PRACTICAL MODELS FOR VISIBILITY FOR GERMAN
LOCATIONS WHERE NO RE. (U) UNIVERSITY OF CENTRAL
FLORIDA ORLANDO DEPT OF MATHEMATICS AND..

1/1

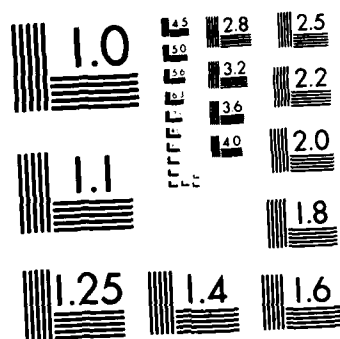
UNCLASSIFIED

P N SONERVILLE ET AL. 03 SEP 82

F/G 4/2

NL





MICROCOPY RESOLUTION TEST CHART
NATIONAL BUREAU OF STANDARDS-1963 A

ADA 126339

AFGL-TR-82-0335

SOME NEW PRACTICAL MODELS FOR VISIBILITY
FOR GERMAN LOCATIONS WHERE NO RECORDS EXIST

P. N. Somerville
S. J. Bean

DEPARTMENT OF MATHEMATICS AND STATISTICS
UNIVERSITY OF CENTRAL FLORIDA
ORLANDO, FLORIDA 32816

Scientific Report No. 3

3 September 1982

Approved for Public Release; Distribution Unlimited

DTIC FILE COPY

AIR FORCE GEOPHYSICS LABORATORY
AIR FORCE SYSTEMS COMMAND
UNITED STATES AIR FORCE
HANSCOM AFB, MASSACHUSETTS 01731

DTIC
SELECTED
APR 4 1983
S A

83 04 04 034

Qualified requestors may obtain additional copies from the
Defense Technical Information Center. All others should
apply to the National Technical Information Service.

| REPORT DOCUMENTATION PAGE | | READ INSTRUCTIONS BEFORE COMPLETING FORM |
|---|-------------------------------------|---|
| 1. REPORT NUMBER AFGL-TR-82-0335 | 2. GOVT ACCESSION NO. AD-A126339 | 3. RECIPIENT'S CATALOG NUMBER |
| 4. TITLE (and Subtitle) Some New Practical Models for Visibility for German Locations Where No Records Exist | | 5. TYPE OF REPORT & PERIOD COVERED Scientific Report No. 3 15 Apr to 3 Sep 82 |
| | | 6. PERFORMING ORG. REPORT NUMBER |
| 7. AUTHOR(s) P. N. Somerville S. J. Bean | | 8. CONTRACT OR GRANT NUMBER(s) F19628-82-K-0001 |
| 9. PERFORMING ORGANIZATION NAME AND ADDRESS Department of Mathematics and Statistics University of Central Florida Orlando, FL 32816 | | 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 62101 F 667009AK |
| 11. CONTROLLING OFFICE NAME AND ADDRESS Air Force Geophysics Laboratory Hanscom AFB, MA 01731 Contract Monitor, D. Grantham LYD | | 12. REPORT DATE 3 Sep 82 |
| | | 13. NUMBER OF PAGES 17 |
| 14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) | | 15. SECURITY CLASS. (of this report) UNCLASSIFIED |
| | | 15a. DECLASSIFICATION/DOWNGRADING SCHEDULE |
| 16. DISTRIBUTION STATEMENT (of this Report) Approved for Public Release, Distribution Unlimited | | |
| 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) | | |
| 18. SUPPLEMENTARY NOTES | | |
| 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Modeling Spreading Evaluation Visibility Sample Reuse Elevation Weibull Distribution Climatological Germany Regression | | |
| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number) Given only month, time of day, and the elevation and surrounding elevations for an arbitrary location in Germany, models are developed for estimating probabilities of visibilities less than a specified distance. The two-parameter Weibull model is used. For a given month and hour period, the parameters are functions of elevation and average elevation of the surrounding region. The models are developed using a somewhat sophisticated nonlinear, least squares regression program. Evaluation is accomplished using 'sample-reuse,' a relatively new technique in which a valid independent evaluation of the model is made using | | |

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)

20. (Continued)

the same observations used to develop the model.

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)

TABLE OF CONTENTS

| | <u>Page</u> |
|--|-------------|
| 1. Introduction | 1 |
| 2. Background of Previous Work on "Spreading" Visibility | 1 |
| 3. Methodology | 3 |
| 4. Use of the Model | 5 |
| 5. Summary | 6 |
| 6. References | 7 |



A

ACKNOWLEDGEMENT

We would like to acknowledge the invaluable assistance of Jon Dittmer, Ken Rodemann, and David Van Brackle in the preparation of this report.

1. Introduction

A goal of the Air Weather Service is to be able to state the probability that a weather element will have a value above a specified threshold for any location at any time. Many models have been developed for modeling such weather elements as visibility, ceiling, sky cover, precipitation, windspeed, etc., for locations where records exist. The modeling for locations where there are no records is a more difficult task. This report develops and evaluates some new models for estimating visibility probabilities for German locations where no records exist. The models require only knowledge of the elevation of the location and the average of the elevations a distance of 20 kilometers from the location in order to estimate visibility probabilities for a specified month and hour period. The next section outlines the work-to-date by the present authors on the problem of predicting visibilities at locations where no records exist.

2. Background of Previous Work on "Spreading" Visibility

At the University of Central Florida, under the sponsorship of the Air Force Geophysical Laboratory, several technical reports have been prepared on the subject of estimating visibility in data void regions, with particular reference to Germany. In AFGL-TR-81-0144, "Some Models for Visibility for German Stations," the Weibull distribution was used to fit visibility data for 30 stations in Germany. For each of the 30 stations, values of α and β were obtained for each month and for all 3-hour periods. For any distance x , the probability $F(x)$ of visibility less than a distance of x miles is then given by the formula

$$F(x) = 1 - e^{-\alpha x^\beta}.$$

Measures of the accuracies of the predictions were also obtained. These, however, were based on the residuals of the least squares fits; and, as such, the standard deviations would be expected to be underestimates. Also, no attempt was made to predict visibility for locations where no records existed.

The first report in which an attempt was made to predict visibility for locations where no records existed was AFGL-TR-81-0313, "Modeling Visibility for Locations in Germany Where No Records Exist." In this report, the models were formulated by using the values for α and β from AFGL-TR-81-0144 and regressing these values on a large number of variables which were potential predictors of the values for α and β . These included such variables as station elevation, relative elevation, proximity to water, mean windspeed and various combinations (interactions) of these and other variables. The prediction equations for α and β were then refined by a sophisticated nonlinear regression program in which the sums of squares of the residuals minimized were not the residual differences between the values for α and β and their predicted values but were the differences between the empirical cumulative distribution function and the model cumulative distribution function. This latter regression produced a set of equations for predicting α and β from geographic and climatic predictor variables. One set of equations was produced for each month and time of day. These models were designated collectively as the "Variables Model."

A second set of models was produced by again using the above mentioned nonlinear regression program; this time using none of the predictor variables. The result was a pair of constants α , β for each month and time of day which gave the best fits for all stations. These models were designated collectively as the "Constants Model."

The measures of accuracy of the models used in this report were the resulting "mean square of the residuals." Since, again, this is essentially an internal estimate and is based on the same data used to produce the models, the RMS values, when interpreted as accuracy measures are optimistic estimates.

The third paper in the series, AFGL-TR-82-0187, "Evaluation of an Observation-based Climatology Model for Predicting Visibility for Data Void Locations in Germany," gives two independent evaluations of the "Constants" model developed in the previous report. Two methods were used. The first was a traditional method. The original 30 stations were regarded as a "calibration" set. A second set of 30 stations was used as an "evaluation" set. The second method involved a relatively new technique called "sample reuse" (also sometimes called cross-

validation), whose use has only recently been made practical due to the availability of "cheap" computing.

The "sample reuse" method evaluations were entirely consistent with the evaluations based on "calibration" and "evaluation" sets, and the report may be said to have confirmed the use of "sample reuse." Values of α and β for the "Constants" model were recalculated making use of all 60 stations.

The report AFGL-TR-82-0239, "Estimating a Family of Distributions with Applications to Climate Spreading," was an attempt to make available to a wider audience some methodologies developed in previous reports and, in particular, the work reported in AFGL-TR-81-0144. The report is an excellent example where the solution of a practical problem resulted in the development of new methodologies and basic research applicable to a much wider class of problems. Publication of this research in the scientific literature is expected.

The present report was first intended to be an independent evaluation of the "Variables" model of AFGL-TR-81-0144. However, since that model included as predictors for α and β variables which would ordinarily not be available for a station where no records existed, and since AFGL-TR-82-0187 demonstrated the ability of "sample reuse" to produce a valid independent evaluation of those models, it was decided to proceed otherwise.

Models were developed for each month and hour period (except hour periods 00-02 and 03-05) using only the variables elevation and relative elevation, whose values would ordinarily be available at locations with no previous records for visibility, and which had previously been confirmed to be useful for prediction purposes. Sample reuse was used to produce independent estimates of the accuracy of the models.

3. Methodology

Let $E_j(x_i)$ be the empirical probability (step function) that the visibility is less than x_i miles for the j^{th} station, using data from the RUSSWOs. The values for x_i are the following distances in miles: $1/4$, $5/16$, $1/2$, $5/8$, $3/4$, 1 , $5/4$, $3/2$, 2 , $5/2$, 3 , 4 , 5 and 6 . Let

$$F_j(x; \alpha_j, \beta_j) = 1 - e^{-\alpha_j x^{\beta_j}}$$

where

$$\alpha_j = \alpha_0 + \alpha_1 * EL_j + \alpha_2 * AE_j$$

$$\beta_j = \delta_0 + \delta_1 * EL_j + \delta_2 * AE_j.$$

EL_j and AE_j are transformed and scaled values for the elevation at station j , and the average elevation at 20 equispaced locations on a circle of radius 20 kilometers and centered at the station. EL is the cube of the elevation in feet, divided by 10^9 . AE is the cube of the average elevation in feet, divided by 10^9 . The constants $\alpha_0, \alpha_1, \alpha_2, \delta_0, \delta_1, \delta_2$ are determined by minimizing the expression

$$\sum_j \sum_i [E_j(x_i) - F_j(x_i; \alpha_j, \beta_j)]^2$$

That is, the constants are those which minimize the sum of squares of the differences between the empirical and model probabilities over all stations and all distance for which data are available. The constants α_0, α_1 and α_2 are given in Exhibit 2.1, "Model Coefficients for Alpha," and the constants $\delta_0, \delta_1, \delta_2$ are given in Exhibit 2.2, "Model Coefficients for Beta."

The models were evaluated by sample reuse. The method of sample reuse may be briefly described as follows. If there are n stations, n separate models are developed. For each model, one station is used as the evaluation set, with the remaining $n-1$ used as the calibration set. For each station, the root mean square (RMS) error of the modeling procedure is obtained. The RMS values for the individual stations are then pooled to obtain an overall RMS error for the procedure. The RMS values by month and hour are given in Exhibit 2.3.

Exhibit 2.4 gives the RMS for each station, averaged over all months and hour periods. The first column of RMS values gives the RMS values from sample reuse, that is, when all of the other stations were

used in the model building process, and the specified station was used as the "evaluation set." The RMS values indicate how well that visibility would have been predicted if the station had been a station "for which no records exist," using a model based on all the other stations. For 54 out of the 60 stations, prediction would have been good. The stations which would not have been well predicted are Baumholder, Siegenberg, Kahler Asten, Plezen, Feldberg and Grosser Falk. The latter six stations have previously presented modeling problems. The second column of RMS values are the RMS values from a full regression for the model using all 60 stations. Two things are remarkable. First, Feldberg and Grosser Falk show up as remarkably influential in the regression. This suggests that for both stations there is a prediction variable that, if used in the model, would have greatly improved prediction for these stations. Second, for the other 58 stations the RMS values are little changed. This suggests (at least to the authors) that the use of the variables of elevation and relative elevation results in a quite good model for predicting visibility probabilities for specific months and hour periods.

Exhibit 2.5 gives the RMS values that resulted when all 60 stations were used to generate the model coefficients given in Exhibits 2.1 and 2.2. These are the RMS values over all stations and are internal estimates. Exhibit 2.3, and not Exhibit 2.5, should be used as a measure of the ability to predict visibility for locations in Germany where no visibility records are available. One reason for retaining Exhibit 2.5 in this report is to indicate that RMS values obtained from the regressions producing the model are overestimates of the model accuracies and instead an independent estimate should be used. It is worth repeating that sample reuse does provide independent estimates of the model accuracies! This is accomplished despite the fact that we do not have two sets of data--one for the determination of the model accuracies and one for the evaluation of the model.

4. Use of the Model

Problem 1: Find α and β for Koblenz for March 0900-1100 hours and use it to find probability of visibility less than 1.5, 2.0 and 6.0

miles. The elevation of Koblenz is 318 feet and the average elevation of the surrounding area is 900 feet.

Solution: From Exhibits 2.1 and 2.2 we have

$$\alpha = .0848 + .00580 (318)^3/10^9 - .00178 (900)^3/10^9 = .0837 \text{ and}$$

$$\beta = 1.26 - .00983 (318)^3/10^9 - .0105 (900)^3/10^9 = 1.252.$$

Estimated probability of visibility less than or equal to x miles is

$$1 - e^{-.0837x^{1.252}}$$

The probabilities of visibilities less than or equal to distances of 1.5, 2.0 and 6.0 miles are thus estimated as .130, .181 and .546. These compare to the RUSSWO values of .090, .156 and .525.

Problem 2: Find α and β for Berus for September 1800-2000 hours and use it to find probabilities of visibility less than 1.5, 2.0 and 6.0 miles. The elevation of Berus is 1204 feet and the average elevation of the surrounding area is 1050 feet.

Solution: From Exhibits 2.1 and 2.2 we have

$$\alpha = .0174 + .00305 x (1204)^3/10^9 - .000689 (1050)^3/10^9 = .0219 \text{ and}$$

$$\beta = 1.40 - .0111 x (1204)^3/10^9 - .00670 (1050)^3/10^9 = 1.373.$$

Estimated probability of visibility less than or equal to x miles is

$$1 - e^{-.0219x^{1.373}}$$

The probabilities of visibilities less than or equal to distances of 1.5, 2.0 and 6.0 miles are thus estimated as .037, .055 and .226. These compare to the RUSSWO values of .019, .027 and .140.

5. Summary

Given only month, time of day, and the elevation and surrounding elevations for an arbitrary location in Germany, models are developed for estimating probabilities of visibilities less than a specified distance. The two-parameter Weibull model is used. For a given month

and hour period, the parameters are functions of elevation and average elevation of the surrounding region. The models are developed using a somewhat sophisticated nonlinear, least squares regression program. Evaluation is accomplished using "sample-reuse," a relatively new technique in which a valid independent evaluation of the model is made using the same observations used to develop the model.

6. References

Bean, S. J. and P. N. Somerville, "Evaluation of Models for 'Spreading' Visibility in Germany," AFGL-TR-82-XXXX, July 1982.

Bean, S. J. and P. N. Somerville, "Estimating a Family of Distributions with Applications to Climate Spreading," AFGL-TR-82-XXXX, 16 August 1982.

Somerville, P. N. and S. J. Bean, "Some Models for Visibility for German Stations," AFGL-TR-81-0144, 15 April 1981. ADA 104167

Somerville, P. N. and S. J. Bean, "Modeling Visibility for Locations in German Where No Records Exist," AFGL-TR-81-0313, December 1981. ADA 111890

LISTING OF EXHIBITS

- Exhibit 2.1 Model Coefficients for α
- Exhibit 2.2 Model Coefficients for β
- Exhibit 2.3 RMS by Month and Hour (Sample Reuse)
- Exhibit 2.4 RMS by Station
 (Col. 1 from Sample Reuse)
 (Col. 2 from Overall Fit)
- Exhibit 2.5 RMS by Month and Hour (Overall Fit)

| Month | Hour Period | | | | | |
|-------|-------------|-----------|-----------|-----------|-----------|-----------|
| | 06-08 | 09-11 | 12-14 | 15-17 | 18-20 | 21-23 |
| Jan | .186 | .212 | .143 | .129 | .131 | .109 |
| | .707e-02 | .598e-02 | .655e-02 | .687e-02 | .713e-02 | .704e-02 |
| | -.154e-02 | -.272e-02 | -.294e-02 | -.278e-02 | -.188e-02 | -.509e-03 |
| Feb | .179 | .176 | .941e-01 | .780e-01 | .831e-01 | .732e-01 |
| | .832e-02 | .717e-02 | .659e-02 | .671e-02 | .697e-02 | .775e-02 |
| | -.500e-02 | -.328e-02 | -.285e-02 | -.274e-02 | -.226e-02 | -.125e-02 |
| Mar | .121 | .848e-01 | .384e-01 | .285e-01 | .307e-01 | .302e-01 |
| | .672e-02 | .580e-02 | .479e-02 | .441e-02 | .510e-02 | .554e-02 |
| | -.164e-02 | -.178e-02 | -.132e-02 | .119e-02 | -.973e-03 | -.139e-02 |
| Apr | .734e-01 | .365e-01 | .204e-01 | .153e-01 | .149e-01 | .144e-01 |
| | .630e-02 | .486e-02 | .409e-02 | .400e-02 | .435e-02 | .433e-02 |
| | -.133e-02 | -.862e-03 | -.107e-02 | -.945e-03 | -.770e-03 | -.654e-03 |
| May | .562e-01 | .235e-01 | .135e-01 | .977e-02 | .107e-01 | .131e-01 |
| | .463e-02 | .399e-02 | .333e-02 | .275e-02 | .322e-02 | .375e-02 |
| | -.114e-02 | -.163e-02 | -.129e-02 | -.894e-03 | -.840e-03 | -.836e-03 |
| Jun | .527e-01 | .215e-01 | .119e-01 | .851e-02 | .898e-02 | .110e-01 |
| | .452e-02 | .370e-02 | .283e-02 | .218e-02 | .275e-02 | .299e-02 |
| | -.720e-03 | -.158e-02 | -.107e-02 | -.621e-03 | -.568e-03 | -.600e-03 |
| Jul | .445e-01 | .186e-01 | .112e-01 | .855e-02 | .843e-02 | .851e-02 |
| | .365e-02 | .310e-02 | .245e-02 | .189e-02 | .205e-02 | .267e-02 |
| | -.187e-03 | -.107e-02 | -.934e-03 | -.527e-03 | -.473e-03 | -.785e-03 |
| Aug | .979e-01 | .278e-01 | .138e-01 | .103e-01 | .101e-01 | .121e-01 |
| | .327e-02 | .282e-02 | .218e-02 | .202e-02 | .239e-02 | .271e-02 |
| | -.118e-02 | -.580e-03 | -.641e-03 | -.482e-03 | -.414e-03 | -.355e-03 |
| Sep | .221 | .706e-01 | .209e-01 | .146e-01 | .174e-01 | .239e-01 |
| | .336e-02 | .352e-02 | .238e-02 | .233e-02 | .305e-02 | .389e-02 |
| | -.230e-02 | -.184e-02 | -.981e-03 | -.738e-03 | -.689e-03 | -.101e-02 |
| Oct | .340 | .194 | .592e-01 | .407e-01 | .628e-01 | .792e-01 |
| | .290e-02 | .388e-02 | .276e-02 | .395e-02 | .428e-02 | .507e-02 |
| | -.411e-02 | -.443e-02 | -.209e-02 | -.165e-02 | -.198e-02 | -.224e-02 |
| Nov | .187 | .170 | .928e-01 | .862e-01 | .942e-01 | .925e-01 |
| | .850e-02 | .752e-02 | .724e-02 | .752e-02 | .794e-02 | .801e-02 |
| | -.311e-02 | -.335e-02 | -.278e-02 | -.272e-02 | -.229e-02 | -.163e-02 |
| Dec | .163 | .184 | .131 | .126 | .126 | .115 |
| | .701e-02 | .589e-02 | .625e-02 | .678e-02 | .689e-02 | .742e-02 |
| | -.146e-02 | -.177e-02 | -.265e-02 | -.228e-02 | -.123e-02 | -.291e-03 |

Exhibit 2.1

Model Coefficients For α

Copy available to DTIC does not
permit fully legible reproduction

| Month | Hour Period | | | | | |
|-------|-------------|-----------|-----------|-----------|-----------|-----------|
| | 06-08 | 09-11 | 12-14 | 15-17 | 18-20 | 21-23 |
| Jan | 1.05 | 1.01 | 1.13 | 1.15 | 1.16 | 1.12 |
| | -.920e-02 | -.872e-02 | -.923e-02 | -.952e-02 | -.105e-01 | -.969e-02 |
| | -.635e-02 | -.600e-02 | -.864e-02 | -.803e-02 | -.522e-02 | -.698e-02 |
| Feb | 1.02 | 1.05 | 1.21 | 1.21 | 1.22 | 1.16 |
| | -.944e-02 | -.892e-02 | -.971e-02 | -.103e-01 | -.108e-01 | -.104e-01 |
| | -.330e-02 | -.564e-02 | -.926e-02 | -.613e-02 | -.443e-02 | -.419e-02 |
| Mar | 1.14 | 1.26 | 1.36 | 1.33 | 1.37 | 1.34 |
| | -.960e-02 | -.983e-02 | -.102e-01 | -.103e-01 | -.111e-01 | -.105e-01 |
| | -.629e-02 | -.105e-01 | -.110e-01 | -.924e-02 | -.708e-02 | -.954e-02 |
| Apr | 1.21 | 1.32 | 1.16 | 1.08 | 1.19 | 1.22 |
| | -.102e-01 | -.923e-02 | -.937e-02 | -.956e-02 | -.107e-01 | -.113e-01 |
| | -.649e-02 | -.159e-01 | -.399e-02 | .483e-03 | -.560e-03 | .143e-02 |
| May | 1.27 | 1.33 | 1.09 | 1.05 | 1.10 | 1.18 |
| | -.876e-02 | -.639e-02 | -.479e-02 | -.566e-02 | -.762e-02 | -.900e-02 |
| | -.193e-01 | -.352e-01 | -.298e-01 | -.218e-01 | -.122e-01 | -.977e-02 |
| Jun | 1.33 | 1.42 | 1.23 | 1.21 | 1.25 | 1.36 |
| | -.812e-02 | -.595e-02 | -.538e-02 | -.803e-02 | -.913e-02 | -.109e-01 |
| | -.265e-01 | -.418e-01 | -.325e-01 | -.145e-01 | -.119e-01 | -.661e-02 |
| Jul | 1.43 | 1.42 | 1.14 | 1.04 | 1.19 | 1.43 |
| | -.889e-02 | -.589e-02 | -.474e-02 | -.766e-02 | -.938e-02 | -.109e-01 |
| | -.724e-01 | -.457e-01 | -.308e-01 | -.388e-02 | -.243e-02 | -.111e-01 |
| Aug | 1.53 | 1.59 | 1.28 | 1.11 | 1.36 | 1.46 |
| | -.100e-01 | -.834e-02 | -.872e-02 | -.855e-02 | -.101e-01 | -.120e-01 |
| | -.245e-02 | -.291e-01 | -.110e-01 | -.316e-02 | -.316e-02 | -.506e-02 |
| Sep | 1.87 | 1.26 | 1.45 | 1.31 | 1.40 | 1.37 |
| | -.727e-02 | -.854e-02 | -.109e-01 | -.973e-02 | -.111e-01 | -.126e-01 |
| | -.232e-02 | -.160e-01 | -.101e-01 | -.296e-02 | -.470e-02 | -.460e-02 |
| Oct | 1.29 | 1.90 | 1.39 | 1.34 | 1.22 | 1.35 |
| | -.620e-02 | -.446e-02 | -.536e-02 | -.464e-02 | -.113e-01 | -.107e-01 |
| | -.546e-02 | -.568e-02 | -.149e-01 | -.108e-01 | -.264e-02 | -.438e-02 |
| Nov | 1.28 | 1.54 | 1.41 | 1.31 | 1.33 | 1.27 |
| | -.710e-02 | -.677e-02 | -.871e-02 | -.740e-02 | -.723e-02 | -.852e-02 |
| | -.211e-02 | -.166e-01 | -.135e-01 | -.166e-02 | -.437e-02 | -.525e-02 |
| Dec | 1.09 | 1.27 | 1.17 | 1.17 | 1.15 | 1.05 |
| | -.560e-02 | -.887e-02 | -.766e-02 | -.763e-02 | -.102e-01 | -.101e-01 |
| | -.176e-02 | -.616e-02 | -.134e-02 | -.890e-02 | -.603e-02 | -.876e-02 |

Exhibit 2.2
Model Coefficients For 8

Co: 7-000-01
Permit 100-1-1

| month | Hour Period | | | | | | ALL |
|-------|-------------|-------|-------|-------|-------|-------|------|
| | 06-08 | 09-11 | 12-14 | 15-17 | 18-20 | 21-23 | |
| Jan | .118 | .111 | .100 | .099 | .115 | .150 | .117 |
| Feb | .102 | .089 | .081 | .081 | .097 | .130 | .089 |
| Mar | .092 | .086 | .079 | .074 | .084 | .098 | .086 |
| Apr | .089 | .078 | .066 | .064 | .072 | .080 | .078 |
| May | .085 | .060 | .040 | .038 | .052 | .069 | .060 |
| Jun | .085 | .055 | .041 | .046 | .057 | .074 | .062 |
| Jul | .087 | .055 | .036 | .041 | .056 | .074 | .061 |
| Aug | .099 | .069 | .055 | .050 | .062 | .088 | .073 |
| Sep | .105 | .079 | .067 | .060 | .079 | .097 | .083 |
| Oct | .096 | .085 | .078 | .078 | .102 | .126 | .096 |
| Nov | .094 | .090 | .074 | .083 | .102 | .125 | .095 |
| Dec | .104 | .102 | .095 | .097 | .107 | .151 | .111 |
| ALL | .097 | .082 | .071 | .070 | .085 | .109 | .087 |

Exhibit 2.3

RMS By Month and Hour (Sample Reuse)

| WMO | Station | Lat (North) | Long (East) | Elev. | Rel Elev. | Sample Re-use RMS | Full Fit RMS |
|-------|----------------------|----------------|----------------|-------|--------------|-------------------------|--------------------|
| 10616 | HAHN AB | 49.95 | 7.27 | 1450. | 1267. | .062 | .048 |
| 10610 | BITBURG AB | 49.95 | 6.57 | 1228. | 1363. | .044 | .042 |
| 10614 | RAMSTEIN AB | 49.43 | 7.58 | 1780. | 710. | .051 | .052 |
| 10607 | SPANGDAHLEH AB | 49.97 | 6.70 | 1196. | 1330. | .057 | .055 |
| 10384 | TEMPELHOF APRT | 52.47 | 13.40 | 164. | 164. | .058 | .058 |
| 10755 | ANSBACH AAF | 49.32 | 10.63 | 1542. | 1181. | .068 | .064 |
| 10544 | FULDA AAF | 50.53 | 9.63 | 1010. | 1650. | .045 | .046 |
| 10869 | ERDING AS | 48.32 | 11.93 | 1522. | 1525. | .064 | .062 |
| 10765 | FEUCHT AAF | 49.38 | 11.18 | 1265. | 1407. | .046 | .045 |
| 10618 | BAUMHOLDER AAF | 49.65 | 7.30 | 1408. | 1538. | .153 | .154 |
| 10626 | BAD KREUZNACH AAF | 49.87 | 7.88 | 355. | 825. | .071 | .071 |
| 10971 | BAD TOLZ AAF | 47.77 | 11.60 | 2360. | 2688. | .121 | .102 |
| 10714 | ZWEIBRÜCKEN AB | 49.22 | 7.40 | 1132. | 938. | .041 | .040 |
| 10633 | WIESBADEN AB | 50.05 | 8.33 | 470. | 617. | .036 | .036 |
| 10633 | FINTHEN AAF | 49.97 | 8.15 | 769. | 948. | .048 | .047 |
| 10763 | FURTH AAF | 49.50 | 10.95 | 1000. | 1225. | .085 | .085 |
| 10542 | HANAU AAF | 50.17 | 8.95 | 377. | 408. | .037 | .036 |
| 10857 | GABLINGEN AAF | 48.45 | 10.87 | 1530. | 1550. | .084 | .082 |
| 10653 | GIEBELSTADT AUX AF | 49.67 | 9.88 | 985. | 950. | .060 | .060 |
| 10687 | GRAFENWOHR AAF | 49.70 | 11.95 | 1370. | 1510. | .063 | .066 |
| 10734 | HEIDELBERG AAF | 49.40 | 8.65 | 369. | 369. | .034 | .034 |
| 10752 | ILLESHEIM AAF | 49.47 | 10.38 | 1060. | 1250. | .084 | .084 |
| 10659 | KITZINGEN AAF | 49.75 | 10.20 | 699. | 899. | .051 | .052 |
| 10763 | MURNBERG | 49.50 | 11.08 | 1053. | 1053. | .062 | .063 |
| 10729 | COLEMAN AAF | 49.57 | 8.47 | 334. | 350. | .078 | .077 |
| 10657 | WERTHEIM AAF | 49.77 | 9.48 | 1120. | 1075. | .095 | .096 |
| 10745 | SCHWABEBISCH HALL AA | 49.17 | 9.78 | 1303. | 1632. | .046 | .046 |
| 10712 | SENBACH AB | 49.52 | 7.87 | 1052. | 1315. | .037 | .037 |
| 10367 | SIEGENBERG GUNNERY | 48.75 | 11.80 | 1325. | 1450. | .140 | .140 |
| 10738 | ECHTERDINGEN ARPT | 48.68 | 9.22 | 1306. | 1200. | .056 | .054 |
| 10501 | AACHEN, DL | 50.78 | 6.12 | 673. | 775. | .081 | .080 |
| 10224 | BREMEN, GER | 53.05 | 8.80 | 502. | 250. | .043 | .043 |
| 10305 | LINGEN, GER | 52.52 | 7.33 | 549. | 250. | .040 | .040 |
| 10427 | KAHLER ASTEN, GER | 51.18 | 8.50 | 3822. | 1563. | .204 | .188 |
| 11157 | AIGEN ENNSTAL, OS | 47.53 | 14.15 | 2139. | 3350. | .056 | .053 |
| 11446 | PLEZEN/DOBRA, CZ | 49.67 | 13.30 | 1194. | 1400. | .130 | .131 |
| 10900 | BREMGARTEN, GER | 47.90 | 7.63 | 699. | 1438. | .044 | .041 |
| 10948 | OBERSIDORF, GER | 47.40 | 10.30 | 2664. | 3350. | .097 | .080 |
| 10929 | KONSTANZ, GER | 47.68 | 9.20 | 1368. | 1725. | .037 | .036 |
| 11120 | INNSBRUCK, OS | 47.27 | 11.37 | 1962. | 3400. | .069 | .074 |
| 11150 | SALZBURG, OS | 47.80 | 13.02 | 1463. | 2338. | .048 | .047 |
| 10893 | PASSAU, GER | 48.58 | 13.50 | 1335. | 1613. | .056 | .055 |
| 10908 | FELDBERG, GER | 47.87 | 8.02 | 4898. | 2550. | .280 | .069 |
| 10921 | NEUHAUSEN, DL | 47.98 | 8.92 | 2648. | 2463. | .072 | .063 |
| 10510 | MURKURG, GER | 50.33 | 6.97 | 2064. | 1425. | .085 | .077 |
| 10515 | KOBLENZ, DL | 50.35 | 7.60 | 318. | 900. | .066 | .068 |
| 10532 | GIESSEN, GER | 50.57 | 8.72 | 640. | 825. | .059 | .060 |
| 10542 | HERSFELD, DL | 50.87 | 9.72 | 738. | 1200. | .059 | .060 |
| 10658 | KISSINLEN, DL | 50.20 | 10.10 | 704. | 1213. | .039 | .040 |
| 10671 | CORBURG, GER | 50.27 | 10.97 | 1106. | 1338. | .038 | .039 |
| 10635 | HOF, GER | 50.32 | 11.90 | 1864. | 1938. | .048 | .057 |
| 10704 | BERUS, GER | 49.27 | 6.70 | 1204. | 1050. | .056 | .054 |
| 10727 | KARLSRUHE, GER | 49.02 | 8.40 | 394. | 600. | .041 | .041 |
| 10742 | OHRRINGEN, GER | 49.20 | 9.53 | 909. | 1075. | .049 | .049 |
| 10788 | STAUBING, GER | 48.82 | 12.60 | 1155. | 1350. | .084 | .085 |
| 10791 | GROSSER FALK, GER | 49.08 | 13.30 | 4291. | 2475. | .259 | .064 |
| 10805 | LAHR, GER | 48.37 | 7.85 | 509. | 800. | .074 | .073 |
| 10837 | LAUDHEIM, GER | 48.22 | 9.93 | 1765. | 1938. | .053 | .056 |
| 10953 | KAUFBEUREN, DL | 47.87 | 10.63 | 2348. | 2513. | .069 | .062 |
| 10875 | MUHLDORF, GER | 48.25 | 12.55 | 1319. | 1625. | .053 | .053 |

Exhibit 2.4

RMS By Station

Hour Region

| Month | 06-08 | 09-11 | 12-14 | 15-17 | 18-20 | 21-23 | All |
|-------|-------|-------|-------|-------|-------|-------|------|
| Jan | .106 | .098 | .086 | .083 | .100 | .140 | .104 |
| Feb | .088 | .074 | .061 | .060 | .079 | .120 | .083 |
| Mar | .075 | .066 | .056 | .048 | .060 | .085 | .066 |
| Apr | .069 | .058 | .041 | .035 | .042 | .053 | .051 |
| May | .068 | .048 | .031 | .026 | .030 | .048 | .044 |
| Jun | .070 | .048 | .031 | .026 | .032 | .047 | .045 |
| Jul | .071 | .046 | .029 | .023 | .030 | .047 | .044 |
| Aug | .082 | .055 | .036 | .028 | .035 | .063 | .053 |
| Sep | .080 | .053 | .030 | .025 | .034 | .073 | .060 |
| Oct | .087 | .071 | .057 | .052 | .081 | .111 | .089 |
| Nov | .082 | .076 | .064 | .060 | .087 | .115 | .083 |
| Dec | .089 | .087 | .079 | .080 | .090 | .142 | .097 |
| All | .083 | .062 | .055 | .051 | .065 | .094 | .071 |

Exhibit 2.5

RMS By Month and Hour (Overall Fit)